A NEW CHARACTERIZATION OF THE GENERALIZED WEIGHTED COMPOSITION OPERATOR FROM H^∞ INTO THE ZYGMUND SPACE

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Abstract. A new criterion for the boundedness, as well as for the compactness of the generalized weighted composition operators from H^∞ into the Zygmund space are given in this paper.

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