SOME REVERSE l_p–TYPE INEQUALITIES INVOLVING CERTAIN QUASI MONOTONE SEQUENCES

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Abstract. In this paper, we give some l_p-type inequalities about sequences satisfying certain quasi monotone type properties. As special cases, reverse l_p-type inequalities for non-negative decreasing sequences are obtained. The inequalities are closely related to Copson's and Leindler's inequalities, but the sign of the inequalities is reversed.

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