A NOTE ON VECTOR–VALUED MAXIMAL MULTILINEAR
OPERATORS AND THEIR COMMUTATORS

ZENGYAN SI AND QINGYING XUE

Abstract. Let T^* be the maximal multilinear Calderón-Zygmund operator with kernels of Dini's type and $T_q^*(\vec{f})$ be the vector-valued version of T^*. In this paper, we consider the weighted norm inequalities for $T_q^*(\vec{f})$. As applications, the weighted strong type and weighted end-point weak type estimates for the commutators of $T_q^*(\vec{f})$ were established respectively.

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