KANTOROVICH PROBLEMS UNDER YOUNG TYPE CONSTRAINTS

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Abstract. We explain how the Hermite-Hadamard inequality agrees with the primal Monge-Kantorovich problems. We also focus onto a particular case of the dual Kantorovich problem, by considering a version significantly affected by some Young type constraints.

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