

UNIMODALITY OF CERTAIN PARAMETRIC INTEGRALS

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Abstract. The unimodality of the functions represented as certain parametric integrals is considered. A crucial part of the proof is based on Kemperman's necessary and sufficient condition for the unimodality of all mixtures of a given family of functions.

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