

ESSENTIAL NORM OF INTEGRAL OPERATORS ON MORREY TYPE SPACES

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Abstract. In this paper, we investigate the essential norm of two classes of integral operators on Morrey type spaces H_K^2 . As an application, we characterize the compactness of these operators.

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