COMPRESSED SAMPLING INEQUALITIES
BY TCHAKALOFF'S THEOREM

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Abstract. We show that a discrete version of Tchakaloff's theorem on the existence of positive algebraic cubature formulas, entails that the information required for multivariate polynomial approximation can be suitably compressed.

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