

A NEW EXTENSION OF CARLSON'S INEQUALITY

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Abstract. A new extension of Carlson's inequality is obtained by using the Euler-Maclaurin summation formula and an extended Beta function introduced recently in [Appl. Math. Comput. 248 (2014) 631–651]. The integral analogue of this inequality is also presented.

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