

A FIEDLER–TYPE THEOREM FOR THE DETERMINANT OF J –POSITIVE MATRICES

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Abstract. In this note we characterize the set of all possible values attained by the determinant of the sum of two J -positive matrices with prescribed spectra, under a natural compatibility condition.

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