ISOPERIMETRIC–TYPE INEQUALITIES
FOR GENERALIZED CENTROID BODIES

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Abstract. We extend the Orlicz centroid body for probability measures to multivariate case and establish the affine isoperimetric-type inequality for the generalized centroid body. Moreover, the concepts of centroid body and mean zonoid are unified through the generalized definition, which is much more significant.

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