

WEIGHTED INEQUALITIES FOR THE GENERALIZED FOURIER TRANSFORM ASSOCIATED WITH THE CHEREDNIK OPERATOR ON THE REAL LINE

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Abstract. We consider the generalized Fourier transform associated with the Cherednik operator on \mathbb{R} and we give the Hardy-Littlewood inequality and some weighted inequalities associated to this transform as particular case, we obtain the analogue of the Pitt's theorem.

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