

## WEIGHTED COMPOSITION OPERATORS FROM DIRICHLET TYPE SPACES TO WEIGHTED TYPE SPACES

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*Abstract.* The boundedness and compactness of weighted composition operators from Dirichlet type spaces to weighted type spaces on the unit ball of  $\mathbb{C}^n$  are characterized in this paper.

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