

ON A PROBLEM CONNECTED WITH STRONGLY CONVEX FUNCTIONS

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Abstract. In this paper we show that the result obtained by Nikodem and Páles in [3] can be extended to a more general case. In particular, for a non-negative function F defined on a real vector space we define F -strongly convex functions and show that such functions are in the form $g + F^*$, where g is a convex function and F^* is a function associated with function F , iff F^* is a quadratic function. Using this result, we get a characterization of quadratic functions.

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