

## ON WEIGHTED INTEGRAL AND DISCRETE OPIAL-TYPE INEQUALITIES

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*Abstract.* In this paper some multidimensional integral and discrete Opial-type inequalities due to Agarwal, Pang and Sheng are considered. Their generalizations and extensions using sub-multiplicative convex functions, appropriate integral representations of functions, appropriate summation representations of discrete functions and inequalities involving means are presented.

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