LOCAL SPECTRAL PROPERTY OF
RELATIVELY REGULAR OPERATORS

Eungil Ko and Mee-Jung Lee

Abstract. In this paper, we study some relatively regular operators T such that $T = TST$ for some $S \in \mathcal{L}(\mathcal{H})$. We give some spectral and local spectral properties between T and S. We also show that some relatively regular operators T have a nontrivial invariant subspace. Finally, we introduce and study the local spectral property of relatively regular operators modulo a nilpotent operator.

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