

A LYAPUNOV–TYPE INEQUALITY FOR A FRACTIONAL DIFFERENTIAL EQUATION UNDER STURM–LIOUVILLE BOUNDARY CONDITIONS

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Abstract. Lyapunov-type inequality is established for a fractional differential equation under Sturm-Liouville boundary conditions. Our results cover many results in the literature.

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