

ON η -CONVEXITY

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Abstract. Some basic inequalities related to η -convex functions are proved. Also we investigate the famous Hermite-Hadamard, Fejer, Jensen and Slater type inequalities for this class of functions. Furthermore some inequalities related to differentiable η -convex functions are obtained as well.

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