

## WEIGHTED COMPOSITION OPERATORS FROM ZYGmund TYPE SPACES INTO BLOCH TYPE SPACES

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*Abstract.* In this paper, we investigate the boundedness and compactness of weighted composition operators from Zygmund type spaces to Bloch type spaces.

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