

## BOUNDS FOR THE ZEROS OF POLYNOMIALS FROM NUMERICAL RADIUS INEQUALITIES

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*Abstract.* We apply matrix norms and recent numerical radius inequalities to a certain Frobenius companion matrix to derive several bounds for the zeros of polynomials. Our results are related to some classical and recent bounds and lead to improve these bounds.

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