

## FRACTIONAL INTEGRAL OPERATORS ON CENTRAL MORREY SPACES

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*Abstract.* We consider the boundedness of fractional integral operators on localized (central) Morrey spaces and investigate the relation between the Adams inequality and the Spanne inequality.

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