

A REMARK ON WEIGHTED INTEGRABILITY

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Abstract. In this paper, we will generalize the result in weighted integrability to include all positive non-integers γ connecting with derivatives of the sum-functions.

Mathematics subject classification (2010): 42A25, 42A50.

Keywords and phrases: Weighted integrability, mean value bounded variation, positivity, monotonicity.

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