INEQUALITIES FOR THE MODIFIED BESSEL
FUNCTION OF THE SECOND KIND AND THE KERNEL
OF THE KRÄTZEL INTEGRAL TRANSFORMATION

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Abstract. We obtain new inequalities for the modified Bessel function of the second kind K_ν in terms of the gamma function. These bounds follow as special cases of inequalities that we derive for the kernel of the Krätzel integral transformation.

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