

## PROOF OF A MONOTONICITY CONJECTURE

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*Abstract.* Bennett gave a generalization of Schur's theorem to study various moment-preserving transformations. In this paper, we confirm a monotonicity conjecture of Bennett which is related to the generalized Schur's theorem and Haber's inequality.

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