# A NOTE ON THE HARDY—LITTLEWOOD
# INEQUALITIES FOR MULTILINEAR FORMS

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*Abstract.* The notion of entropy of the Hardy–Littlewood inequalities for multilinear forms was introduced and explored by Pellegrino and Teixeira in [14]. In this note, among other results, we introduce a related notion and obtain some new estimates.

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