

ESSENTIAL NORM OF WEIGHTED COMPOSITION OPERATORS ON ZYGMUND-TYPE SPACES WITH NORMAL WEIGHT

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Abstract. In this paper, we investigate the boundedness, compactness and essential norm of weighted composition operators between Zygmund-type spaces with normal weight.

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