A SHARPENING OF A PROBLEM ON BERNSTEIN
POLYNOMIALS AND CONVEX FUNCTIONS

ULRICH ABEL AND IOAN RAŞA

Abstract. We present an elementary proof of a conjecture by I. Raşa which is an inequality involving Bernstein basis polynomials and convex functions. It was affirmed in positive very recently by the use of stochastic convex orderings.

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