

SOME NEW INTEGRAL INEQUALITIES ON TIME SCALES

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Abstract. In this paper, we establish some generalizations of inequalities on time scales, which have appeared in different articles. The inequalities that we will derive from our results when $g(t) = t$ are essentially new.

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