

EQUIVALENT INTEGRAL CONDITIONS RELATED TO BILINEAR HARDY-TYPE INEQUALITIES

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Abstract. Infinitely many, even scales of, equivalent conditions are derived to characterize the bilinear Hardy-type inequality under various ranges of parameters.

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