

WEIGHTED COMPOSITION OPERATORS FROM WEIGHTED BERGMAN SPACES TO STEVIĆ-TYPE SPACES

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Abstract. The boundedness, compactness and essential norm of weighted composition operators from weighted Bergman spaces with a double weight to Stević-type spaces on the unit disk are investigated in this paper.

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