THE OSTROWSKI TYPE INEQUALITIES WITH THE APPLICATION TO THE THREE POINT INTEGRAL FORMULA

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Abstract. The generalization of the integral formula with three nodes is introduced, and some sharp and the best possible inequalities for the functions whose higher order derivatives belong to L_p spaces are given. We establish non-weighted version of the three point integral formula. From the general non-weighted formula we shall get the famous Simpson, dual Simpson and Maclaurin formulae. Some new errors of approximation in these integral formulae are obtained.

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