LOCAL ONE–SIDED MAXIMAL FUNCTION
ON FRACTIONAL SOBOLEV SPACES

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Abstract. In this article we study the boundedness of local one sided maximal operators on weighted fractional Sobolev Spaces. As a consequence we obtain a Lebesgue differentiation theorem for functions in fractional Sobolev spaces.

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