DUAL COMPLEMENTS FOR DOMAINS OF $\mathbb{C}^n$

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Abstract. Let $\Omega \subset \mathbb{C}^n$ be a bounded, strictly convex domain and $\widetilde{\Omega}$ be its dual complement. Very few such domains with fully described dual complements have been known. We present new types of domains for which their dual complements can be completely described.

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