

HIGHER-DIMENSIONAL WEIGHTED KNOPP TYPE INEQUALITIES

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Abstract. We give a necessary and sufficient condition on weight pairs for a class of higher-dimensional weighted Knopp type inequalities to hold. The corresponding result for the multivariate adjoint Hardy type operator is obtained.

Mathematics subject classification (2010): 26D15, 26D10.

Keywords and phrases: Knopp type inequality, weight, Hardy inequality, adjoint Hardy type operator.

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