

HERMITE–HADAMARD INEQUALITY FOR A FRUSTUM OF A SIMPLEX

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Abstract. In this paper, we establish a refinement of the Hermite-Hadamard inequality for convex functions of several variables defined on a frustum of a simplex.

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