CONTINUOUS FORMS OF GAUSS–PÓLYA TYPE
INEQUALITIES INVOLVING DERIVATIVES

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Abstract. The main aim of this paper is to give a continuous form of the Gauss-Pólya type inequalities i.e. to give inequalities involving infinitely many functions. We consider inequalities which involve derivatives and which structure is related to the Hölder inequality. Also, some properties of the corresponding functionals are given.

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