

CONVERSE TO THE SHERMAN INEQUALITY WITH APPLICATIONS

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Abstract. In this paper we proved a converse to Sherman's inequality. Using the concept of f -divergence we obtained some inequalities for the well-known entropies. We also introduced a new entropy by applying the Zipf-Mandelbrot law and derived some related inequalities.

Mathematics subject classification (2010): 94A17, 26D15, 15B51.

Keywords and phrases: Sherman inequality, Majorization inequality, Jensen inequality, f -divergence, Zipf-Mandelbrot entropy, convex function.

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