

ON AN OPEN PROBLEM OF FENG QI AND BAI-NI GUO

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Abstract. In this work, we investigate an open problem posed by Feng Qi and Bai-Ni Guo in their paper "Complete monotonicities of functions involving the gamma and digamma functions [7]".

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