

MAJORIZATION AND REFINEMENTS OF HERMITE–HADAMARD INEQUALITY

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Abstract. In this note we use majorization methods to derive and analyze refinements of Hermite–Hadamard inequality for a convex function.

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