

MIXED INVEX EQUILIBRIUM PROBLEMS WITH GENERALIZED RELAXED MONOTONE AND RELAXED INVARIANT PSEUDOMONOTONE MAPPINGS

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Abstract. In this paper, we introduce generalized relaxed monotone mappings and relaxed invariant pseudomonotone mappings for bi-functions. By using KKM technique, we establish certain existence results for mixed invex equilibrium problems with the generalized relaxed monotone mappings and some of the results for invex equilibrium problems with the relaxed invariant pseudomonotone mappings in Banach spaces.

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