OPTIMAL BOUNDS OF THE ARITHMETIC MEAN
IN TERMS OF NEW SEIFFERT–LIKE MEANS

MONIKA NOWICKA AND ALFRED WITKOWSKI

Abstract. We provide the optimal bounds for the arithmetic mean in terms of the arithmetic, harmonic, quadratic, inverse quadratic and geometric combination of means generated by sine, tangent, hyperbolic sine and hyperbolic tangent functions.

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