

WEIGHTED ITERATED DISCRETE HARDY-TYPE INEQUALITIES

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Abstract. Necessary and sufficient conditions on functions u and ω are established ensuring boundedness of a discrete Hardy-type operator from a weighted sequence space $l_{p,u}$ to a weighted sequence space for a wide range of the numerical parameters p, u and θ .

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