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BOUNDS OF NUMERICAL RADIUS OF BOUNDED LINEAR OPERATORS USING t–ALUTHGE TRANSFORM

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Abstract. We develop a number of inequalities to obtain bounds for the numerical radius of a bounded linear operator defined on a complex Hilbert space using the properties of t-Aluthge transform. We show that the bounds obtained are sharper than the existing bounds.

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