

NEW NORM EQUALITIES AND INEQUALITIES FOR CERTAIN OPERATOR MATRICES

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Abstract. We prove new norm equalities and inequalities for general $n \times n$ tridiagonal and anti-tridiagonal operator matrices, including pinching type inequalities for weakly unitarily invariant norms.

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