

COVERING FUNCTIONALS OF MINKOWSKI SUMS AND DIRECT SUMS OF CONVEX BODIES

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Abstract. We prove a series of inequalities concerning covering functionals of convex bodies having the form $K + L$, where K is a convex body and L is a segment. Several estimations of covering functionals of direct sums of convex bodies are also presented.

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