ON SOME PROPERTIES OF THE CARATHÉODORY FUNCTIONS

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Abstract. We find a sufficient condition for an analytic function in $|z| < 1$ to be with positive real part in $|z| < 1$. It follows sufficient conditions for a function to be convex, starlike, etc. These conditions describe the boundary behavior of the functions on $|z| = r < 1$.

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