

TRIGONOMETRIC APPROXIMATION OF FUNCTIONS IN SEMINORMED SPACES

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Abstract. In this paper, we study the approximation properties of 2π -periodic functions in a seminormed space. We use a general matrix method of summability, and the moduli of continuity in the seminormed space as a measure of approximation. Our results generalize and improve some of the previous results available in the literature.

Mathematics subject classification (2010): 41A25, 46E30, 42A24, 42A10, 40C05.

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