CONVERGENCE IN MEASURE OF FEJÉR MEANS OF
TWO PARAMETER CONJUGATE WALSH TRANSFORMS

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Abstract. Weisz proved-among others – that for $f \in L \log L$ the Fejér means $\widetilde{\sigma}_{n,m}^{(t,u)}$ of conjugate transform of two-parameter Walsh-Fourier series a. e. converges to $f^{(t,u)}$. The main aim of this paper is to prove that for any Orlicz space, which is not a subspace of $L \log L$, the set of functions for which Walsh-Fejér Means of two parameter Conjugate Transforms converge in measure is of first Baire category.

Mathematics subject classification (2010): 42C10.
Keywords and phrases: Double Walsh-Fourier series, conjugate transform, convergence in measure.

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