

## A NOTE ON WEIGHTED ESTIMATES FOR BILINEAR FRACTIONAL INTEGRAL OPERATORS

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*Abstract.* De Napoli, Drelichman and Durán (2011) proved weighted estimates for the fractional integral operators. Komori-Furuya and Sato (2020) proved weighted estimates for bilinear fractional integral operators. We show that their results are optimal by giving counterexamples.

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