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ON GENERALIZED LEAST POWER APPROXIMATION

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Abstract. We study generalized least power approximation corresponding to certain sets of seminorms on Banach spaces. As applications, we construct sets of seminorms for trivariate harmonic polynomials and for Müntz polynomials such that the sequences of the generalized least power approximations converge uniformly.

Mathematics subject classification (2020): 41A10, 41A63, 41A65.

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