

## INEQUALITIES FOR QUERMASSTINTEGRALS OF (NEW) $p$ -PARALLEL BODIES

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*Abstract.* In this paper, we define a new family of convex bodies related to the family of  $p$ -parallel bodies, which is determined by the 0-extreme normal vectors, and establish some inequalities for their quermassintegrals.

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